

AUC apCalculus BC

Assignment 14 (Review Assignment 01)

PROBLEM 7.4. Study the convergence of the following series:

$$(1) \sum_{n=1}^{+\infty} \frac{1}{(5n+4)^6}.$$

$$(2) \sum_{n=1}^{+\infty} \sin^5\left(\frac{n^3+1}{n^{3.5}+4\sin(n^n)}\right).$$

$$(3) \sum_{n=1}^{+\infty} \frac{e^{4n}}{(n+2)!}.$$

$$(4) \sum_{n=1}^{+\infty} \frac{n!}{e^{3n^2}}.$$

$$(5) \sum_{n=1}^{+\infty} \sin^2\left(\frac{7^n}{8^n}\right).$$

PROBLEM 8.1. Study the convergence of the following series:

$$(1) \sum_{n=1}^{+\infty} \frac{n^3 - \cos(e^n)n+1}{5n^5+1}.$$

$$(2) \sum_{n=1}^{+\infty} \frac{5n^{100} \cdot 7^n}{2^{3n}}.$$

$$(3) \sum_{n=1}^{+\infty} \sin^7\left(\frac{n^3+1}{n^{3.2}+4\sin(n^n)}\right).$$

$$(4) \sum_{n=1}^{+\infty} \frac{n!}{n^{50}e^{2n}}.$$

$$(5) \sum_{n=1}^{+\infty} \frac{1}{n^2} - \frac{1}{(n+1)^2}.$$

$$(6) \sum_{n=1}^{+\infty} \frac{1}{n \ln^2(n)}.$$

$$(7) \sum_{n=1}^{+\infty} \sin(n).$$

PROBLEM 10.1. Study the convergence of the following series:

$$(1) \sum_{n=1}^{+\infty} \frac{n^2-1}{(3n-1)^7}.$$

$$(2) \sum_{n=1}^{+\infty} \sin^3\left(\frac{n^2+1}{n^{2.1}+4\sin(e^n)}\right).$$

$$(3) \sum_{n=1}^{+\infty} \frac{n^5 n!}{e^{n^2}}.$$

$$(4) \sum_{n=1}^{+\infty} \frac{1}{n(n+1)(n+2)}.$$

$$(5) \sum_{n=1}^{+\infty} \frac{2^{n+2} - 3^{n+4}}{10^n}.$$

$$(6) \sum_{n=1}^{+\infty} \frac{6^n}{7^n}.$$

$$(7) \sum_{n=1}^{+\infty} \frac{1}{n \ln^3(n)}.$$

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11. On Absolute and Conditional Convergence, Alternating Series and their Error Theorems

PROBLEM 11.1. (70 points) Study the convergence of the following series:

$$(1) \sum_{n=1}^{+\infty} \frac{(-1)^n(6n+11)}{2n^2+7}.$$

$$(2) \sum_{n=1}^{+\infty} (-1)^n e^{-n^3}.$$

$$(3) \sum_{n=1}^{+\infty} \frac{(-1)^n}{n^{8/9}}.$$

$$(4) \sum_{n=1}^{+\infty} \frac{(-1)^n}{\sqrt{n+3}}.$$

$$(5) \sum_{n=1}^{+\infty} (-1)^n \sin\left(\frac{1}{n}\right).$$

$$(6) \sum_{n=1}^{+\infty} (-1)^{n^2} n^2 \left(1 - \cos\left(\frac{1}{n}\right)\right).$$

PROBLEM 11.2. (15 points)

- (1) Give the definition of Alternating series.
- (2) Give the definition of Conditionally convergent series.
- (3) Give the definition of Absolutely convergent series.
- (4) State the Theorem that relates Absolute convergence and Convergence.
- (5) Give the definition of a Cauchy sequence.
- (6) Give the statement of the Alternating series test and its Error formula.

PROBLEM 11.3. (15 points)

Find a rational approximation of the following limits within an error of $\frac{1}{10000}$

$$(1) \sum_{n=1}^{+\infty} (-1)^n \frac{1}{n!}.$$

$$(2) \sum_{n=1}^{+\infty} (-1)^n \frac{1}{n^2}.$$