

**APPC Lesson 2.6 Homework**

Name \_\_\_\_\_

1. Write the equations for the vertical asymptotes of the graph of

$$f(x) = \frac{3}{(x+4)(x-10)}.$$

2. For a rational function  $m$ ,  $\lim_{x \rightarrow -9^-} m(x) = 2$  and  $\lim_{x \rightarrow -9^+} m(x) = 2$  but  $m(-9)$  is undefined. Does the graph of  $m$  have a hole, a vertical asymptote, or neither at  $x = -9$ ? Explain.

3. Let  $f(x) = \frac{(x-9)(x+2)}{(x+2)(x+4)}$ . Where does the graph of  $f$  have a vertical asymptote?

4. Find the domain of  $g(x) = \frac{x^2 - 16}{x^2 + x - 12}$

5. Let  $f(x) = \frac{(x-a)(x-b)}{(x-b)(x-c)}$  for some constants  $a, b,$  and  $c$  where  $a \neq b \neq c$ .

Which of the following statements is FALSE?

A) The graph of  $f$  has exactly one  $x$ -intercept at  $x = a$ .

B) The domain of  $f$  is  $\{x \in \mathbb{R} | x \neq b, c\}$ .

C) The graph of  $f$  has a vertical asymptote at  $x = b$  and a hole at  $x = c$ .

D) The graph of  $f$  has a horizontal asymptote at  $y = 1$ .

6. Let  $f(x) = \frac{x^2 - 7x + 10}{x^2 - 3x - 40}$ .

a. Find the  $x$ -intercept(s) of the graph of  $f$ .

b. Write the equation(s) of any vertical asymptote(s) on the graph of  $f$ .

c. Find the  $y$ -intercept of the graph of  $f$ .

d. Find the ordered pair(s) of any holes on the graph of  $f$ .

e. Write the equation of any horizontal asymptotes of  $f$  or explain why none exist.

-  7. Compare the functions  $f(x) = \frac{(x+1)(x+5)}{x+1}$  and  $g(x) = x+5$ .
- Are the domains the same?
  - Which of the functions, if any, has a vertical asymptote?
  - Use a calculator to graph both functions. What is the same? What is different?

8. The graph of a function  $f$  is shown. Which of the following could define the function  $f$ ?

A)

$$f(x) = \frac{(x + 2)(x - 5)(x - 3)}{4(x - 2)(x - 3)}$$

B)

$$f(x) = \frac{(x - 2)(x + 5)(x + 3)}{4(x + 2)(x + 3)}$$

C)

$$f(x) = \frac{(x + 2)(x - 5)(x - 2)}{4(x - 2)(x - 5)}$$

D)

$$f(x) = \frac{(x + 2)(x - 2)(x - 5)}{4(x - 2)(x - 3)}$$

