

Reteaching

Problem

Elimination is one way to solve a system of equations. Think about what the word “eliminate” means. You can eliminate either variable, whichever is easiest.

$$4x - 3y = -4$$

Solve and check the following system of linear equations.

$$2x + 3y = 34$$

Solution The equations are already arranged so that like terms are in columns.

Notice how the coefficients of the y -variables have the opposite sign and the same value.

$$\begin{array}{r} 4x - 3y = -4 \\ 2x + 3y = 34 \\ \hline 6x = 30 \\ x = 5 \end{array}$$

Add the equations to eliminate y .

Divide both sides by 6 to solve for x .

$$\begin{array}{r} 4(5) - 3y = -4 \\ 20 - 3y = -4 \\ -3y = -24 \\ y = 8 \end{array}$$

Substitute 5 for x in one of the original equations and solve for y .

The solution is $(5, 8)$.

Check

$$\begin{array}{r} 4x - 3y = -4 \\ 4(5) - 3(8) \stackrel{?}{=} -4 \\ 20 - 24 \stackrel{?}{=} -4 \\ -4 = -4 \checkmark \end{array}$$

Substitute your solution into both of the original equations to check.

You can check the other equation.

Exercises

Solve and check each system. **SHOW ALL YOUR WORK!!!** Use a separate sheet of paper to show work.

1. $3x + y = 3$

$$-3x + y = 3$$

2. $6x - 3y = -14$

$$6x - y = -2$$

3. $3x - 2y = 10$

$$x - 2y = 6$$

4. $4x + y = 8$

$$x + y = 5$$

Reteaching (continued)

If none of the variables has the same coefficient, you have to multiply before you eliminate.

Problem

Solve the following system of linear equations.

$$\begin{aligned} -2x + 3y &= -1 \\ 5x + 4y &= 6 \end{aligned}$$

Solution

$$\begin{aligned} 5(-2x - 3y) &= (-1)5 \\ 2(5x + 4y) &= (6)2 \end{aligned}$$

Multiply the first equation by 5 (all terms, both sides) and the second equation by 2. You can eliminate the x variable when you add the equations together.

$$\begin{array}{r} -10x - 15y = -5 \\ 10x + 8y = 12 \\ \hline -7y = 7 \end{array}$$

Distribute, simplify and add.

$$\begin{aligned} y &= -1 \\ 5x + 4(-1) &= 6 \end{aligned}$$

Divide both sides by 7.
Substitute -1 in for y in the second equation to find the value of x .

$$\begin{aligned} 5x - 4 &= 6 \\ 5x &= 10 \\ x &= 2 \end{aligned}$$

Simplify.
Add 4 to both sides.
Divide by 5 to solve for x .

The solution is $(2, -1)$.

Check $-2x + 3y = -1$

Substitute your solution into both original equations.

$$\begin{aligned} -2(2) - 3(-1) &= -1 \\ -4 + 3 &= -1 \\ -1 &= -1 \quad \checkmark \end{aligned}$$

You can check the other equation.

Exercises

Solve and check each system. **SHOW ALL YOUR WORK!!!** Use a separate sheet of paper to show work.

5. $x - 3y = -3$

6. $-2x - 6y = 0$

$-2x + 7y = 10$

$3x + 11y = 4$

7. $3x + 10y = 5$

8. $4x + y = 8$

$7x + 20y = 11$

$x + y = 5$