

# 5-6 Reteaching

Nonvertical lines are parallel if they have the same slope and different  $y$ -intercepts. The graphs of  $y = 2x - 6$  and  $y = 2x + 3$  are parallel because they have the same slope, 2, but different  $y$ -intercepts,  $-6$  and  $3$ .

## Problem

What is an equation in slope-intercept form of the line that passes through  $(8, 7)$  and is parallel to the graph of  $y = \frac{3}{4}x + 2$ ?

The slope of  $y = \frac{3}{4}x + 2$  is  $\frac{3}{4}$ . Because the desired equation is for a line parallel to a line with slope  $\frac{3}{4}$ , the slope of the parallel line must also be  $\frac{3}{4}$ . Use the slope and the given point in the point-slope form of a linear equation and then solve for  $y$  to write the equation in slope-intercept form.

$y - y_1 = m(x - x_1)$	Start with the point-slope form
$y - 7 = \frac{3}{4}(x - 8)$	Substitute $(8, 7)$ for $(x_1, y_1)$ and $\frac{3}{4}$ for $m$ .
$y - 7 = \frac{3}{4}x - 6$	Distributive Property
$y = \frac{3}{4}x + 1$	Add 7 to each side.

The graph of  $y = \frac{3}{4}x + 1$  passes through  $(8, 7)$  and is parallel to the graph of  $y = \frac{3}{4}x + 2$ .

## Exercises

1. **Writing** Are the graphs of  $y = \frac{2}{5}x + 3$  and  $y = \frac{3}{5}x - 4$  parallel? Explain how you know.

Write an equation in slope-intercept form of the line that passes through the given point and is parallel to the graph of the given equation.

2.  $(3, 1)$ ;  $y = 2x + 4$       3.  $(1, 3)$ ;  $y = 7x + 5$       4.  $(1, 6)$ ;  $y = 9x - 5$

5.  $(0, 0)$ ;  $y = -\frac{1}{2}x - 4$       6.  $(-5, 7)$ ;  $y = -\frac{2}{5}x - 3$       7.  $(6, 6)$ ;  $y = \frac{1}{3}x - 1$

**Reteaching**

(continued)

**5-6**

Two lines that are neither horizontal nor vertical are perpendicular if the product of their slopes is  $-1$ . The graphs of  $y = -\frac{4}{5}x - 5$  and  $y = \frac{5}{4}x + 4$  are perpendicular because  $-\frac{4}{5}(\frac{5}{4}) = -1$ .

**Problem**

What is an equation in slope-intercept form of the line that passes through  $(2, 11)$  and is perpendicular to the graph of  $y = \frac{1}{4}x - 5$ ?

The slope of  $y = \frac{1}{4}x - 5$  is  $\frac{1}{4}$ . Since  $\frac{1}{4}(-4) = -1$ , the slope of the line perpendicular to the given line is  $-4$ .

Use this slope and the given point to write an equation in point-slope form. Then solve for  $y$  to write the equation in slope-intercept form.

$$\begin{array}{ll} y - y_1 = m(x - x_1) & \text{Start with the point-slope form} \\ y - 11 = (-4x - 2) & \text{Substitute } (2, 11) \text{ for } (x_1, y_1) \text{ and } -4 \text{ for } m. \\ y - 11 = -4x + 8 & \text{Distributive Property} \\ y = -4x + 19 & \text{Add 11 to each side.} \end{array}$$

The graph of  $y = -4x + 19$  passes through  $(2, 11)$  and is perpendicular to the graph of  $y = \frac{1}{4}x - 5$ .

**Exercises**

**8. Writing** Are the graphs of  $y = \frac{2}{3}x + 6$  and  $y = -\frac{3}{2}x - 4$  parallel, perpendicular, or neither? Explain how you know.

**Write an equation in slope-intercept form of the line that passes through the given point and is perpendicular to the graph of the given equation.**

9.  $(5, -3)$ ;  $y = 5x + 3$

10.  $(4, 8)$ ;  $y = -2x - 4$

11.  $(-2, -5)$ ;  $y = x + 3$

12.  $(6, 0)$ ;  $y = \frac{3}{2}x - 6$

13.  $(5, 3)$ ;  $y = 5x + 2$

14.  $(7, 1)$ ;  $y = -\frac{7}{2}x + 6$